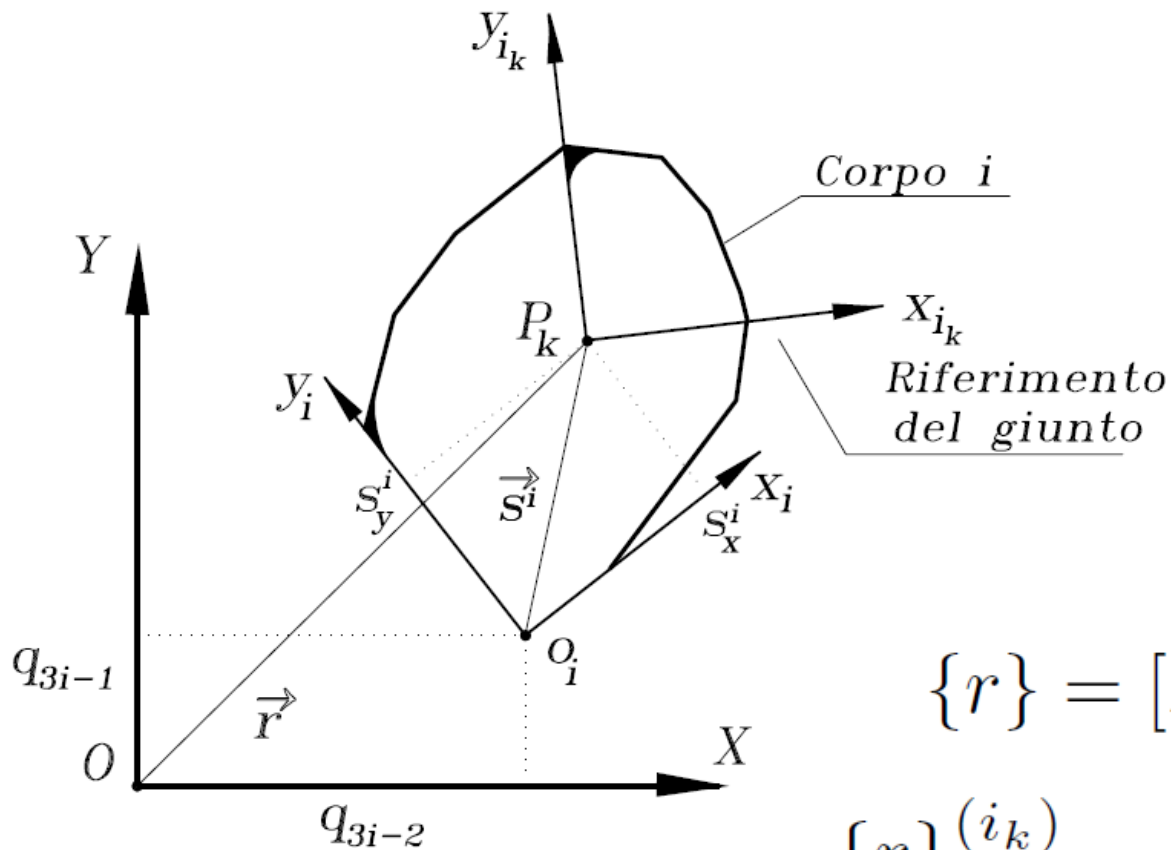




$$\begin{aligned}\{\ddot{q}\} + [\Psi_q]^T \{\lambda\} &= \{F_e\} \ , \\ [\Psi_q] \{\ddot{q}\} &= \{\gamma\}\end{aligned}$$



$$\{r\} = [A_i] [C_{i_k}^i] \{r\}^{(i_k)} ,$$

$$\{r\}^{(i_k)} = [C_{i_k}^i]^T [A_i]^T \{r\} .$$

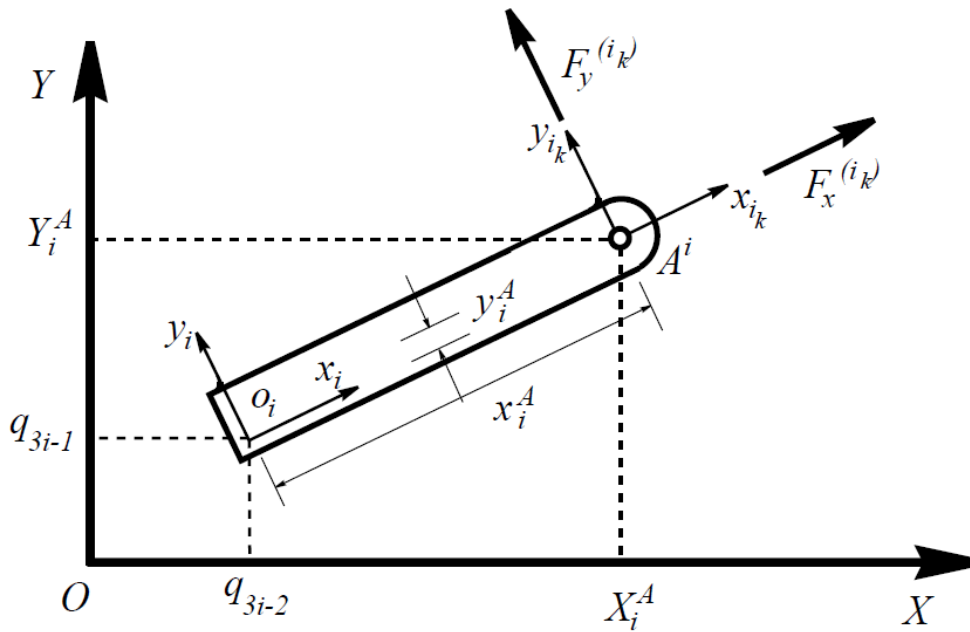
$$\delta W_0 = - \left\{ \delta q_{3i-2} \quad \delta q_{3i-1} \quad \delta q_{3i} \right\} \begin{bmatrix} \Psi_{q_{3i-2}}^k & \Psi_{q_{3i-2}}^{k+1} \\ \Psi_{q_{3i-1}}^k & \Psi_{q_{3i-1}}^{k+1} \\ \Psi_{q_{3i}}^k & \Psi_{q_{3i}}^{k+1} \end{bmatrix} \left\{ \begin{array}{c} \lambda_k \\ \lambda_{k+1} \end{array} \right\},$$

$$\delta W_{i_k} = \left\{ \delta r_x^{(i_k)} \quad \delta r_y^{(i_k)} \right\} \left\{ \begin{array}{c} F_x^{(i_k)} \\ F_y^{(i_k)} \end{array} \right\} + \delta q_{3i} T_z^{(i_k)}$$

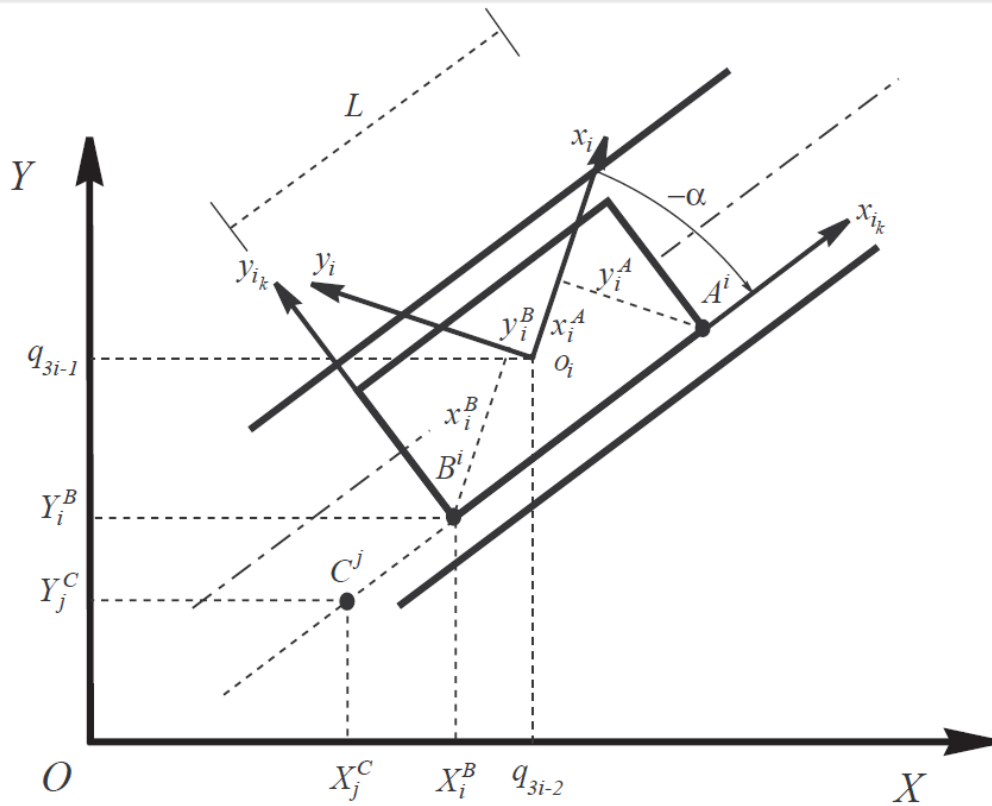
$$\{r\} = \left\{ \begin{array}{c} q_{3i-2} \\ q_{3i-1} \end{array} \right\} + [A_i] \left\{ \begin{array}{c} s_x^{(i)} \\ s_y^{(i)} \end{array} \right\},$$

$$\left\{ \begin{array}{c} F_x^{(i_k)} \\ F_y^{(i_k)} \end{array} \right\} = - [C_{i_k}^i]^T [A_i]^T \begin{bmatrix} \Psi_{q_{3i-2}}^k & \Psi_{q_{3i-2}}^{k+1} \\ \Psi_{q_{3i-1}}^k & \Psi_{q_{3i-1}}^{k+1} \end{bmatrix} \left\{ \begin{array}{c} \lambda_k \\ \lambda_{k+1} \end{array} \right\}, \quad (9)$$

$$T_z^{(i_k)} = \left(\left\{ \begin{array}{c} s_x^{(i)} \\ s_y^{(i)} \end{array} \right\} [B_i]^T \begin{bmatrix} \Psi_{q_{3i-2}}^k & \Psi_{q_{3i-2}}^{k+1} \\ \Psi_{q_{3i-1}}^k & \Psi_{q_{3i-1}}^{k+1} \end{bmatrix} - \left[\Psi_{q_{3i}}^k \quad \Psi_{q_{3i}}^{k+1} \right] \right) \left\{ \begin{array}{c} \lambda_k \\ \lambda_{k+1} \end{array} \right\} \quad (10)$$



$$\begin{Bmatrix} F_x^{(i_k)} \\ F_y^{(i_k)} \\ T_z \end{Bmatrix} = - \begin{Bmatrix} \lambda_k \cos q_{3i} + \lambda_{k+1} \sin q_{3i} \\ -\lambda_k \sin q_{3i} + \lambda_{k+1} \cos q_{3i} \\ 0 \end{Bmatrix} .$$

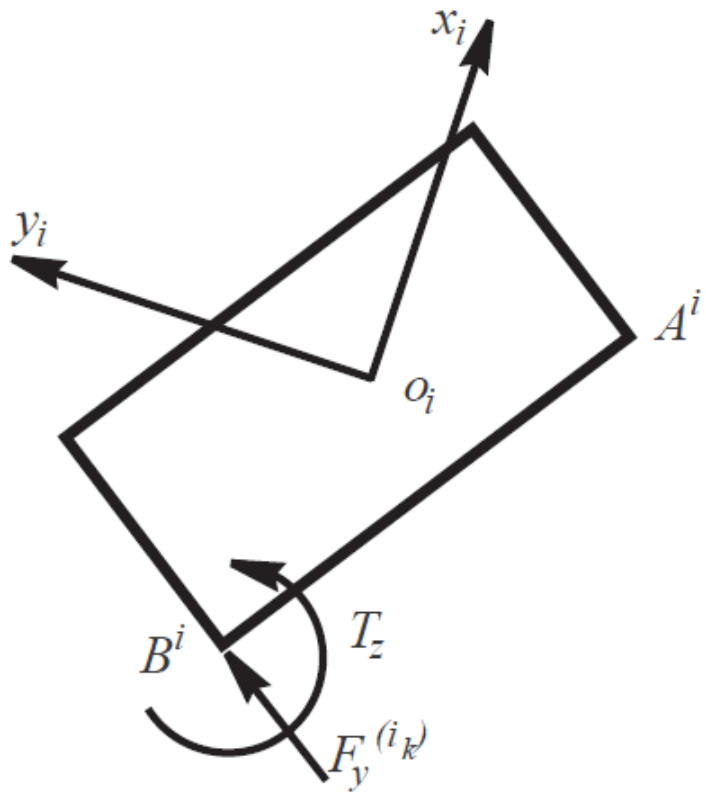


$$\begin{Bmatrix} F_x^{(i_k)} \\ F_y^{(i_k)} \\ T_z \end{Bmatrix} = \begin{Bmatrix} K_1 \\ K_2 \\ K_3 \end{Bmatrix},$$

$$K_1 = 0 ,$$

$$K_2 = \lambda_k \left[(Y_i^B - Y_i^A) \sin (q_{3i} + \alpha) - (X_i^A - X_i^B) \cos (q_{3i} + \alpha) \right]$$

$$K_3 = \lambda_k \left[(q_{3i-1} - Y_i^B) (Y_i^B - Y_i^A) \right. \\ \left. + (X_i^B - q_{3i-2}) (X_i^A - X_i^B) - H_1 \right] - \lambda_{k+1} .$$



$$\begin{aligned} [M] \{\ddot{q}\} + [\Psi_q]^T \{\lambda\} &= \{F\} \\ \{\Psi(q, t)\} &= \{0\} . \end{aligned}$$

$$[\Psi_q] \{\ddot{q}\} = \{\gamma\}$$



$$\begin{bmatrix} M & \Psi_q^T \\ \Psi_q & 0 \end{bmatrix} \begin{Bmatrix} \ddot{q} \\ \lambda \end{Bmatrix} = \begin{Bmatrix} F_e \\ \gamma \end{Bmatrix}, \quad (14)$$

$$\{\dot{q}\}_{(i+1)\Delta t} = \{\dot{q}\}_{i\Delta t} + \{\ddot{q}\}_{i\Delta t} \Delta t ,$$

$$\{q\}_{(i+1)\Delta t} = \{q\}_{i\Delta t} + \{\dot{q}\}_{i\Delta t} \Delta t + \frac{1}{2} \{\ddot{q}\}_{i\Delta t} \Delta t^2$$